

1. Find the derivative of  $y = x^2$  with respect to  $\ln x$ .
2. Find the derivative of  $y^2$  with respect to  $x^4$  if  $y = \sqrt{x^2 + 5}$
3. Simplify  $e^{4 \ln x}$
4. Find  $\frac{dy}{dx}$  if  $y = 3^{x+1}$
5. Find  $\frac{dy}{dx}$  if  $y = (\ln x)^x$
6. Find  $\frac{dy}{dx}$  if  $y = \sqrt{4x^2 + 4x}$
7. Find  $\frac{dy}{dx}$  if  $y = \cos x \sin x$
8. Find  $\frac{dy}{dx}$  if  $y = \cos^3 5x$
9. Find  $\frac{dy}{dx}$  if  $y = \ln(xe^{2x})$
10. Which of the following functions does not have a derivative equal to  $\frac{1}{x}$ ?
- $\ln(ex)$
  - $\ln(2x)$
  - $\ln(e^{\ln x})$
  - $\ln(xe^x)$
11. Write the equation of the tangent line to  $f(x) = e^{2x}$  at  $x = 2$ .
12. Find  $\frac{dy}{dx}$  if  $y = \ln(6x^2 - 3)$
13. Simplify  $e^{4x+2 \ln x}$
14. Find  $\frac{dy}{dx}$  if  $y = \ln |\sin 3x|$
15. Find  $\frac{dy}{dx}$  if  $y = 2^{\cos x}$
16. Find  $\frac{dy}{dx}$  if  $y = \ln\left(\frac{x^2}{e^{6x}}\right)$
17. Find  $\frac{dy}{dx}$  if  $y = x^2 \sec 4x$
18. Find the derivative of  $y = x^3 + 2x^2$  with respect to  $\cos x$ .
19. Find  $\frac{dy}{dx}$  if  $y = x^{\cot 2x}$
20. Find  $\frac{dy}{dx}$  if  $y = \cos^2(3x) + \sin^2(3x)$

**Answers:**

1. $2x^2$	2. $\frac{1}{2x^2}$	3. $x^4$
4. $3^{x+1} \ln 3$	5. $(\ln x)^x \left[ \frac{1}{\ln x} + \ln(\ln x) \right]$	6. $\frac{2x+1}{\sqrt{x^2+x}}$
7. $\cos 2x$	8. $-15 \cos^2 5x \sin 5x$	9. $\frac{1+2x}{x}$
10. D	11. $y - e^4 = 2e^4(x - 2)$	12. $\frac{4x}{2x^2 - 1}$
13. $x^2 e^{4x}$	14. $3 \cot 3x$	15. $-2^{\cos x} (\ln 2)(\sin x)$
16. $\frac{2-6x}{x}$	17. $2x \sec 4x(1 + 2x \tan 4x)$	18. $\frac{-3x^2 - 4x}{\sin x}$
19. $\left( -2 \ln x \csc^2 2x + \frac{\cot 2x}{x} \right) x^{\cot x}$	20. 0	